# Department of Mathematics 

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Faculty<br>Professor: Bradie, Chen, Martin<br>Associate Professor: Dobrescu, Kennedy<br>Assistant Professor: Fogarty, J. P. Kelly, J. S. Kelly, Kuster, Morena, Panayotova, Samuels<br>Lecturer: Lenhart, Nailor, J. Perry<br>Instructor: Carpenter, Tong<br>Emeriti: Avioli, Bartels, Kostaki-Gailey, Summerville

## Mission Statement

As a department within a university that values liberal learning, our mission is to provide high-quality programs that challenge students to appreciate the power, utility and beauty of mathematics. Outstanding teaching is the hallmark of the Department of Mathematics, in addition to maintaining vigorous program in research and service. Major and minor programs offered by the department prepare students for professional careers or further study.

## Expected Outcomes

- To instill in students an appreciation for the power and relevance of mathematics as it relates to life,
- To equip students with a solid foundation in theoretical and applied mathematics necessary for advanced study or a professional career,
- To build foundational skills in critical thinking, reasoning, and problem solving,
- To help students develop their individual mathematical interests through internships, independent study, or faculty-student research,
- To provide students with mathematical proficiency to be successful when taking courses in other disciplines such as physics, computer science, engineering, biology, chemistry, biochemistry, neuroscience, psychology, sociology, and business.

The Department of Mathematics offers a variety of courses for those who wish to develop general or specific skills in mathematics, to satisfy the mathematics liberal learning foundation, to study mathematics for aesthetic reasons, or to pursue a Bachelor of Arts or Bachelor of Science degree in mathematics or a minor in mathematics.

Historical and philosophical highlights related to the development of mathematics are discussed in various mathematics major courses. Also, the ability to write computer programs is a prerequisite for MATH 335. Because of the
complexity of planning a long-term program for students intending to major or minor in mathematics, especially for those intending to teach mathematics in Virginia secondary schools, students are encouraged to consult with the Department of Mathematics before registering for courses. This applies to both degree and non-degree seeking students.

## Calculus Placement

Students intending to register for either MATH 135-Calculus for Business and Social Sciences, MATH 140-Calculus and Analytic Geometry or MATH 148- Accelerated Calculus must have the appropriate prerequisite course (either MATH 110 or MATH 130 for MATH 135; MATH 130 for MATH 140) or receive a passing score on the Calculus Readiness Assessment (CRA). The CRA is administered at Setting Sail and prior to the registration period each semester. Any student intending to major in mathematics, applied physics, computer science, computer engineering, information systems, information science, chemistry, business or economics should take the CRA as soon as possible. The CRA is also offered every semester during the week before registration for the subsequent semester. A student's placement score is good for one academic year. For more information, see the departmental website.

## Online Homework

Many mathematics courses use an online homework system. After selecting a particular class section, students should check the Captain's Locker to determine what software may be required. Students will need to purchase access using the provided ISBN on the Captain's Locker website.

## Overrides

Students seeking an override for a closed course or to waive prerequisites must receive the approval of the department chair.

## General Requirements for all Math Degrees

All students planning to pursue either the Bachelor of Arts or the Bachelor of Science in mathematics must satisfy the liberal learning curriculum, complete the Major Field Test, and all general requirements for graduation. All courses must be chosen in consultation with an academic advisor. Students may have no more than two grades below $C$ - in courses applied toward the major.

## Bachelor of Arts Degree in Mathematics

In addition to the successful completion of the liberal learning curriculum, students seeking a Bachelor of Arts in mathematics must successfully complete the following courses:

1. Minimum grade of C- in MATH 140 or 148 and 240 ;
2. MATH 128 or 3 credits in CPSC numbered 125 or higher;
3. MATH $245,250,260,360,370$;
4. Either MATH 451 or MATH 499;
5. Complete 21 credits at the $300-400-\mathrm{level}$ :
a. Select 12 MATH credits at the 300-400 level (excluding MATH 301,451 ); at least 3 credits must be at the 400 level (excluding 451, 490, 499);
b. Select nine credits at the $300-400$ level in MATH (excluding MATH 301W, 308, 451 and 499) or in one of the following disciplines: PHYS, CHEM, CPSC, CPEN, ECON, NEUR, BIOL, or BCHM. Courses must be chosen in consultation with the advisor or department chair.

## Bachelor of Science Degree in Mathematics

In addition to the successful completion of the liberal learning curriculum, students seeking a Bachelor of Science in mathematics must successfully complete the following courses:

1. Minimum grade of C- in MATH 140 or 148 and 240 ;
2. CPSC 150/150L;
3. PHYS 201/201L and PHYS 202/202L;
4. MATH $245,250,260,360,370,375$;
5. MATH 460 or 470 ;
6. MATH 451 or 499 ;
7. Complete 15 MATH credits satisfying the following requirements:
a. Six credits must form a sequence, chosen from the following list of options:
1) MATH 320 and either MATH 410 or 420 ;
2) MATH 335 and MATH 435;
3) Two of MATH 330, 345, and 373;
4) MATH 350 and MATH 355 ;
5) MATH 380 and MATH 440;
6) MATH 365 and MATH 378.
b. Select nine MATH credits at the 300-400 level (excluding MATH $301 \mathrm{~W}, 303 \mathrm{~W}$, and 451).

## Bachelor of Science degree, Computational and Applied Mathematics Major

Applied mathematics is the application of mathematics to real-world problems. It is inherently multi-disciplinary. The primary objective of the computational and applied mathematics (CAM) program is to provide a degree where students integrate their interest and ability in mathematics with a complementary interest in an applied discipline. Another important objective of the CAM program is to prepare students for a career or graduate school by combining
the CNU liberal learning curriculum with a rigorous mathematics core and a substantive investigation into their chosen application field.

## Bachelor of Science degree, Computational and Applied Mathematics Major Biology and Life Sciences Concentration

In addition to the successful completion of the liberal learning curriculum, students seeking a Bachelor of Science in computational and applied mathematics, biology and life sciences concentration, must successfully complete the following courses:

1. Minimum grade of C- in MATH 140 or 148 and 240;
2. MATH 250, 260, 320, 360, 440;
3. MATH 451 or MATH 499;
4. Select two: CPSC 270, PHYS 341, or any 300-400 level MATH (excluding 301W, 440, 451, 490 and 499). Recommended selections are CPSC 270, MATH 335 or 380 ;
5. CPSC $150 / 150 \mathrm{~L}$ and either CPSC $250 / 250 \mathrm{~L}$ or 255 ;
6. BIOL 211/211L, 213/213L, 313, and 326;
7. CHEM $121 / 121 \mathrm{~L}, 122 / 122 \mathrm{~L}$.

## Bachelor of Science degree, Computational and Applied Mathematics Major <br> Computational Chemistry Concentration

In addition to the successful completion of the liberal learning curriculum, students seeking a Bachelor of Science in computational and applied mathematics, computational chemistry concentration, must successfully complete the following courses:

1. Minimum grade of C- in MATH 140 or 148 and 240 ;
2. MATH $250,260,320,360,440$;
3. PHYS 201/201L and 202/202L;
4. MATH 451 or MATH 499 ;
5. Select two: CPSC 270, PHYS 341, or any 300-400 level MATH (excluding 301W, 440, 451, 490 and 499). Recommended selections are CPSC 270 and either MATH 335 or 380;
6. CPSC $150 / 150 \mathrm{~L}$ and either CPSC $250 / 250 \mathrm{~L}$ or 255 ;
7. CHEM $121 / 121 \mathrm{~L}, 122 / 122 \mathrm{~L}, 321 / 321 \mathrm{~L}, 341,342 / 342 \mathrm{~L}$;
8. CHEM 395 Computational Chemistry;

## Bachelor of Science degree, Computational and Applied Mathematics Major <br> Economics Concentration

In addition to the successful completion of the liberal learning curriculum, students seeking a Bachelor of Science in computational and applied mathematics, economics concentration, must successfully complete the following courses:

1. Minimum grade of C- in MATH 140 or 148 and 240;
2. MATH 250, 260, 320, 360, 440 ;
3. MATH 451 or MATH 499;
4. Select two: CPSC 270, PHYS 341, or any 300-400
level MATH (excluding 301W, 440, 451, 490 and 499).
Recommended selections are CPSC 270, and either
MATH 335 or 380;
5. CPSC $150 / 150 \mathrm{~L}$ and either CPSC $250 / 250 \mathrm{~L}$ or 255 ;
6. MATH 125 or 435 ;
7. ECON 201, 202, 485;
8. ACCT 201;
9. FINC 300;
10. Select three credits at the 300-400 level in ECON.
11. One sequence from the following list to satisfy the University Bachelor of Science Degree Requirement. No more than three lecture courses may be taken from the same discipline, and no more than two laboratory courses may be taken from the same discipline to satisfy the University Bachelor of Science Degree Requirement and the Investigating the Natural World Area of Inquiry.

BIOL 107, 108, 109L
BIOL 211/211L-212/212L
BIOL 211/211L-213/213L
CHEM 103/103L - 104/104L
CHEM 121/121L - 122/122L
PHYS 151/151L-152/152L
PHYS 201/201L-202/202L

## Bachelor of Science degree, Computational and Applied Mathematics Major

Physics, Dynamics and Engineering Concentration
In addition to the successful completion of the liberal learning curriculum, students seeking a Bachelor of Science in computational and applied mathematics, physics, dynamics and engineering concentration, must successfully complete the following courses:

1. Minimum grade of C- in MATH 140 or 148 and 240;
2. MATH 250, 260, 320, 360, 440;
3. MATH 451 or MATH 499;
4. Select two: CPSC 270, PHYS 341, or any 300-400 level MATH (excluding 301W, 440, 451, 490 and 499). Recommended selections are CPSC 270, and either MATH 335 or 380;
5. CPSC $150 / 150 \mathrm{~L}$ and either CPSC $250 / 250 \mathrm{~L}$ or 255 ;
6. PHYS 201/201L, 202/202L, 303, 340;
7. Select one: CPEN 214, ENGR 211/211L, or 213;
8. Select three credits at the 300-400 level in PHYS or CPEN.

## The Minor in Discrete Mathematics (19 credits)

To complete the minor in discrete mathematics, students must complete the following:

1. MATH 140 with a $C$ - or higher;
2. MATH 245 and either MATH 235 or MATH 260 with a $C$ - or higher;
3. Nine additional credits from the following list: MATH 330, MATH 345, MATH 370, MATH 373, MATH 375, MATH 390, or MATH 470.

## The Minor in Mathematics (19-20 credits)

The minor in mathematics requires successful completion of the following:

1. MATH 140 or 148 , with a $C$ - or higher;
2. MATH 240 and 260 , with a $C$ - or higher;
3. MATH 245 or 250 , with a $C$ - or higher;
4. Six additional MATH credits at the 300 - or 400 -level.

## Teacher Preparation in Mathematics

Those students who wish to become licensed teachers should apply to the five-year Master of Arts in Teaching (M.A.T.) program. Application to the program must be made in spring of the junior year. See the Graduate Catalog for application instructions and requirements. Students will earn either a B.A. or B.S. in mathematics after the first four years and then take an additional year of studies leading to an M.A.T. degree. The courses and degree requirements for the M.A.T. are found in the graduate catalog. Students accepted into this program must complete one of the following tracks for graduation with the bachelor's degree:

## Elementary level (PK-6) Track

Major courses as required for the B.A. or B.S. in Mathematics. Support courses required:

- ENGL 123, 223, 310 or 430, and 316;
- COMM 201 or THEA 230
- CPSC 110;
- MATH 109, 125;
- HIST 111, 121, 122;
- POLS 101;
- GEOG 210;
- PSYC 208, 312;
- SOCL 314/314L;
- BIOL 107 or 108; CHEM 103; PHYS 141; PHYS 105L or BIOL 109L;
- NSCI 310.

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## Secondary level (6-12) Track: Math endorsement

Major courses as required for either the B.A. or the B.S. in Mathematics and MATH 378.
Support courses required:

- CPSC 110;
- MATH 125 and 378;
- PSYC 207 or 208 and 312;
- SOCL 314/314L;
- COMM 201 or THEA 230 .
- B.S. degree candidates must take PHYS 201-202 with the accompanying laboratories.

Graduate courses* required (senior year):

- MATH 555, 538 or PSYC 544.
*See the graduate catalog for course descriptions. The Praxis II exam should be taken soon after completing Math 125, 240, and 245.


## The Curriculum in Mathematics

## MATH 109. Theoretical Foundations of Elementary School Mathematics (3-3-0)

Prerequisite: PSYC 207 or 208 or SOCL 314.
Spring.
Strongly recommended for prospective elementary school teachers, this course covers concepts and theories underlying fundamental mathematics. Topics include sets, logic, number sentences, introduction to number theory, number systems, intuitive geometry and measurement.

## MATH 110. College Algebra (3-3-0)

Restricted to freshman standing or approval of the chair. This course is designed for those students who intend to take MATH 130 or MATH 135 and do not have adequate algebra skills for these courses. Topics include real number properties, exponents, polynomial and rational expressions, equations and inequalities, functions, quadratic functions, and logarithms. Students may not receive credit for this course after receiving a grade of $C$ - or higher in MATH 130 , or any course numbered MATH 135 or higher.

MATH 115. Contemporary Mathematics (3-3-0) LLFM Prerequisite: Through Algebra II in high school.
This course is designed to introduce the student to applications of mathematics, including finance, linear programming (optimization problems), systems of equations, and other topics. Students may not receive credit for this course after receiving a grade of $C$-or higher in any course numbered MATH 250 or higher.

## MATH 120. The Saga of Mathematics (3-3-0) LLFM

Prerequisite: Through Algebra II in high school.
An introduction to the history of mathematics, concentrating on the period from the Greeks through the 19th century. This course shows the history and development of mathematics as a vital and integral part of the history of civilization, including the history of numbers and numerals, computation, geometry, algebra, trigonometry, calculus and modern mathematics.

## MATH 125. Elementary Statistics (3-3-0) LLFM

Prerequisite: Through Algebra II in high school.
This course is a general survey of descriptive and inferential statistics. Topics include descriptive analysis of univariate and bivariate data, probability, standard distributions, sampling, estimation, hypothesis testing and linear regression. Students may not receive credit for this course after receiving a grade of $C$ - or higher in MATH 435.

MATH 127. Elementary Cryptography (3-3-0) LLFM
This course examines elementary cryptographic methods, ranging from early Caesar cipher to modern day RSA encryption. Modular arithmetic and how it can be used for cryptographic methods is studied. Cryptanalysis of the resulting methods will also be studied. No previous experience with cryptography or the underlying mathematics is assumed. While not required, a laptop computer is beneficial in this class. Students may not receive credit for this course after receiving a grade of $C$ - or higher in CPSC 428.

## MATH 128. Introduction to Mathematical Programming (3-3-0) LLFM

This course will introduce the student to mathematical programming, in which researchers use a high-level programming language (e.g., Mathematica) to model, analyze, visualize and calculate numeric, geometric and symbolic data. In addition, it is designed for the student to take early so that he or she will have a powerful tool to use in subsequent courses in many disciplines. Specific topics include programming, logic, visualization, sets, sums, products, loops, substitution, patterns, and matrices.
MATH 130. Precalculus (3-3-0) LLFM
Prerequisite: Through Algebra II in high school.
Designed for the student planning to take calculus, MATH 140, but who has insufficient knowledge of analytic geometry, trigonometry, and functions. Topics include real numbers, inequalities, analytic geometry, linear and quadratic functions, polynomials and rational functions, trigonometry, and exponential and logarithmic functions. Students may not receive credit for this course after receiving a grade of $C$ - or higher in any course numbered MATH 250 or higher.

## MATH 131. Mathematics for the Life Sciences (3-3-0) LLFM

This course is intended for biology majors to satisfy the second half of the Mathematical Literacy requirement, as well as anyone with an interest in the life sciences. Topics will include: model building and parameter estimation through regression analysis of life tables and analysis of matrix population models. Concepts of growth rate, halflife and doubling time, elasticity, life expectancy, stable age distribution and reproductive value will be discussed. No specialized knowledge of biology is required.

## MATH 135. Calculus for Business and Social Sciences (3-3-0) LLFM

Prerequisite: A minimum grade of C- in MATH 110 or 130 or an acceptable score on the Calculus Readiness Assessment. An introduction to the calculus of functions arising in business and the social sciences. Exponential and logarithmic functions, differentiation, and integration. Modeling and applications will be stressed. Students may not receive credit for this course after receiving a grade of $C$ - or higher in any course numbered MATH 250 or higher.

## MATH 140. Calculus and Analytic Geometry (4-4-1) LLFM

Prerequisite: A minimum grade of C-in MATH 130 or an acceptable score on the Calculus Readiness Assessment.
An introduction to the calculus of elementary functions, continuity, derivatives, methods of differentiation, the Mean Value Theorem, curve sketching, applications of the derivative, the definite integral, the Fundamental Theorems of Calculus, indefinite integrals, and logarithmic and exponential functions. The software package Mathematica will be used.

## MATH 148. Accelerated Calculus (3-3-0) LLFM

Prerequisite: An acceptable score on the Calculus
Readiness Assessment and consent of Department Chair. Fall.
Accelerated version of MATH 140 for students who have been exposed to calculus in high school. Students cannot receive credit for MATH 148 after receiving a grade of C- or higher in MATH 140, or if grade of $C$ - or higher has been earned in any course numbered 250 or higher or their equivalent.

## MATH 195. Special Topics (3-3-0)

As needed.
Topics vary, determined by the special interests and needs of students and the expertise of faculty.
MATH 235. Applied Matrix Techniques (3-3-0)
Prerequisite: MATH 135; or 140 or 148, CPSC 125 or 150/150L.
Fall and as needed in Spring.
Topics in applied linear algebra such as systems of linear equations, Gaussian elimination, matrix algebra, determinants, Cramer's rule, eigenvalues and vectors. Also applications in some of these areas: linear programming, game theory, Markov chains, input/output models, graph theory, and genetics. A computer project may be required.

## MATH 240. Intermediate Calculus (4-4-0)

Prerequisite: A minimum grade of $C$ - in either MATH 140 or 148.
Techniques of integration, L'Hospital's Rule, application of integration, approximations, Taylor's Theorem, sequences and limits, series of numbers and functions, power series, and Taylor series. The software package Mathematica will be used.

MATH 245. Proofs and Discrete Mathematics (3-3-0) [Formerly MATH 310, equivalent]
Prerequisite: MATH 140 with a grade of C- or better.
Topics are presented so as to develop facility with methods of proof and mathematical argument. Topics will include logic, sets, binary relations, functions, elementary number theory, mathematical induction, and other topics at the discretion of the instructor.

MATH 250. Multivariable Calculus (3-3-0)
Prerequisite: A minimum grade of C- in MATH 240.

An introduction to the calculus of real-valued functions of more than one variable. The geometry of three-space, vectorvalued functions, partial and directional derivatives, multiple and iterated integrals, and applications. The software package Mathematica will be used.

## MATH 260. Linear Algebra (3-3-0)

Prerequisite: C- or higher in either MATH 240 or MATH 245. Systems of linear equations, matrix operations, determinants, vectors and vector spaces, independence, bases and dimension, coordinates, linear transformations and matrices, eigenvalues and eigenvectors.

## MATH 295. Special Topics (credits vary 1-3)

Prerequisite: As announced.
Topics vary, determined by the special interests and needs of students and the expertise of faculty.

## MATH 301. WI: Writing in Mathematics I (1-1-0)

Prerequisite: ENGL 223, MATH 240 with a C-or higher and junior standing.
This course consists of multiple writing assignments, exposing students to various types of mathematical and technical writing. The mathematical typesetting language, LaTeX, is introduced and used throughout the course. This course partially satisfies the writing intensive requirement.

## MATH 303. WI: Mathematics in Context (1-1-0)

Prerequisite: MATH 301 and at least one MATH course at 320 or higher with a $C$ - or higher.
Through reading and writing assignments, students will consider the importance of audience and venue as it relates to effectively communicating mathematics results. Each course will have a particular mathematical focus. Students will be expected to complete a variety of mathematical and writing assignments. This course partially satisfies the writing intensive requirement.

## MATH 320. Ordinary Differential Equations (3-3-0)

Prerequisite: A minimum grade of C - in MATH 240.
A first course in ordinary differential equations and their applications. Topics will include existence and uniqueness of solutions; techniques for the qualitative analysis of autonomous equations; the numerical and analytical methods, including the method of Laplace Transforms, for finding solutions for certain classes of equations.

## MATH 330. Graph Theory and Combinatorics (3-3-0)

Prerequisite: A minimum grade of C- in MATH 245.
Spring, odd numbered years.
This course will emphasize the basic methods of enumeration, up to generating functions. It also will strive to apply learned counting methods to the central objects of combinatorics, such as permutations, graphs, and hypergraphs. If time permits, this course will cover some special topics that will provide the students with a closer view of research problems.

## MATH 335. Applied Probability (3-3-0)

Prerequisite: A minimum C-in MATH 240, a minimum C-in at least one of MATH 128, CPSC 125, 130L or 150
Fall.
Elementary probability theory including combinatorics, distributions of random variables, conditional probability, and moment generating functions. An introduction to stochastic processes including such topics as Markov chains, random walks, and queuing theory. Case studies may be considered. Computer projects may be required.

## MATH 345. Number Theory (3-3-0)

Prerequisite: A minimum grade of C- in MATH 245.
Spring, even numbered years.
Topics include prime numbers, linear Diophantine equations, congruencies, theorems of Fermat, Wilson, and Euler, and numbers in other bases.

## MATH 350. Vector Calculus (3-3-0)

Prerequisite: A minimum grade of C- in MATH 250.
Spring, even numbered years.
An introductory course in differential and integral vector calculus. Topics include vector operations, gradients, divergence, curl, line integrals, Green's Theorem, Stokes' Theorem, Divergence Theorem, and applications.

## MATH 355. Complex Variables (3-3-0)

Prerequisite: A minimum grade of C- in MATH 250.
Spring, odd numbered years.
Introduction to the calculus of complex variables and its application to applied mathematics, physics and engineering. Topics include analytic functions, Cauchy-Reimann equations, residues and poles, and conformal mappings.

MATH 360. Real Analysis I (3-3-0)
Prerequisite: A minimum grade of C- in MATH 250 and 260. MATH 245 is recommended.
A first course in real analysis covering various topics including point-set topology, continuity, differentiability, the Riemann integral, sequences of functions, series of functions, Taylor and Fourier series, uniform continuity and uniform convergence.

## MATH 365. Topology (3-3-0)

Prerequisite: A minimum grade of C- in MATH 245.
Fall, even numbered years.
A first course in point-set topology. Topics include the definition of a topology, closed sets, continuous functions, convergence, metric spaces, connectedness, compactness, and separation axioms.

## MATH 370. Modern Algebra I (3-3-0)

Prerequisite: A minimum grade of C- in MATH 245 and 260. Fall.
This is an introduction to binary operations and algebraic structures. Concentrating on group theory, topics include
abstract groups, abelian groups, permutation groups, homomorphisms and quotient groups. This is a proof-based course, stressing both concrete and theoretical concepts in algebra.

## MATH 373. Coding and Information (3-3-0)

Prerequisite: A minimum grade of $C$ - in one of MATH 245, MATH 260, or ENGR 213.
Spring, odd numbered years.
Error correcting codes are means of transmitting information over noisy channels that allow for limited correction without re-transmission. The course covers vector spaces over finited fields and progresses to a survey of error-correcting codes, emphasizing applications and decoding algorithms.

MATH 375. Linear Algebra and its Applications (3-3-0) Prerequisite: A minimum grade of C- in MATH 260.
This course is a continuation of Math 260. Math 245 with a minimum grade of C - is recommended. While emphasizing theory, this course will include appropriate applications. Starting with a systematic study of general vector spaces over $\mathbf{R}$ and $\mathbf{C}$, the course progresses to bilinear forms, inner product spaces, the Gram-Schmidt process, linear functionals, dual spaces and Eigentheory over $\mathbf{R}$ and $\mathbf{C}$. Applications such as QR-decompositions, singular value decomposition, least squares and regression, Fourier series, and the Jordan canonical form will be covered as time allows.

## MATH 378. Elementary Geometry from an Advanced Standpoint (3-3-0)

[Formerly MATH 578, equivalent]
Prerequisite: MATH 245 with a grade of C- or higher Spring.
This course compares and contrasts the origins, applications and basic structures of Euclidean and non-Euclidean geometry. Attention is given to ideas involved in teaching geometry.

## MATH 380. Numerical Analysis I (3-3-0)

Prerequisite: A minimum grade of C-in MATH 240 and 260. Fall, odd numbered years.
A survey of numerical methods for scientific and engineering problems. Topics will include: rootfinding techniques, polynomial and spline interpolation, numerical differentiation and integration and the numerical solution of initial value problems for ordinary differential equations. Consideration will be given to theoretical concepts and to efficient computation procedure. Computer projects will be required.

## MATH 390. Operations Research (3-3-0)

Prerequisite: A minimum grade of C- in MATH 260.
Fall, even numbered years.
A study of the nature, scope, applications, and theoretical basis of operations research. The simplex algorithm, duality theory, applications of graph theory, and heuristic algorithms. Computer projects may be required.

## MATH 395. Special Topics (credits vary 1-3)

Prerequisite: As announced.
Topics vary, determined by the special interests and needs of students and the expertise of faculty.

## MATH 410. Advanced Ordinary Differential Equations

 (3-3-0)Prerequisite: MATH 320.
Fall, even numbered years.
A second course in ordinary differential equations. Topics will be selected from: series solutions near singular points, systems of first-order linear equations, nonlinear differential equations and autonomous systems, equilibria and stability, bifurcations, existence and uniqueness theory, chaotic behavior, Sturm-Liouville theory, and numerical methods.

## MATH 420. Partial Differential Equations (3-3-0)

Prerequisite: MATH 320 and 360.
Fall, odd numbered years.
Discussion of methods used in solving problems arising from continuous mathematical models. An introduction to partial differential equations. Additional topics may include: Sturm-Liouville Theory and qualitative theory of ordinary differential equations, transform methods, Green's functions, delay differential equations, special functions, and numerical methods.

## MATH 435. Mathematical Statistics (3-3-0)

Prerequisite: MATH 335.
Spring, even numbered years.
A study of the nature, scope, and theoretical basis of methods of estimation, hypothesis testing, and statistical decision making. Descriptive statistics, quality of estimators and best tests, techniques of estimation and hypothesis testing, and regression analysis. Additional topics such as analysis of variance, non-parametric procedures, sampling techniques and MINITAB. Computer projects may be required.

MATH 440. Mathematical Modeling (3-3-0)
Prerequisite: MATH 320 and 360.
Spring.
Modeling and solution of some problems that arise in the sciences. Emphasis on development of appropriate models and an awareness of their domain of applicability.

## MATH 451. Independent Learning Experience (1-1-0)

Prerequisite: either MATH 360 or 370.
Spring.
This course is designed to introduce students to techniques for effectively communicating mathematical reasoning and content and to provide students with the opportunity to demonstrate their ability to study some area of mathematics beyond what the student sees in the standard mathematics curriculum under faculty advisement. Students will perform independent reading of multiple sources and prepare small written summaries of each reading and will communicate
their findings both in the form of an oral presentation and a written report.

## MATH 460. Real Analysis II (3-3-0)

Prerequisite: MATH 360.
Spring, odd numbered years.
This is a continuation of Math 360. Topics will include metric spaces, continuous functions on metric spaces, uniform convergence, power series, Fourier series, multi-variable differential calculus along with Lebesgue measure theory and Lebesgue integration.

## MATH 470. Modern Algebra II (3-3-0)

Prerequisite: MATH 370.
Spring, even numbered years.
This course is a continuation of Math 370 . Topics will include rings, fields, field extensions, and polynomial rings over fields. Additional topics may include Galois theory, unique factorization, principal ideal, Euclidean domains, and noncommutative examples.

## MATH 490. Internship in Mathematics

Prerequisite: Mathematics major, CPSC 150/150L, MATH
360, nine semester hours in MATH at 300 or 400 level, 3.00
GPA in 300 and 400 level courses and internship director approval.
40 clock hours ( 60 minute hours) of scheduled, on-site time required for each semester hour of credit earned. Course may be repeated up to a maximum of three credits. A projectbased experience in a private, governmental, or military organization that permits an intern to apply mathematics to a project of mathematical substance and gain appropriate experience in a mathematically-related employment environment. This course is graded Pass/fail.

## MATH 495. Special Topics (credits vary 1-3)

Prerequisite: As announced.
Topics vary, determined by the special interests and needs of students and the expertise of faculty.

MATH 499. Independent Research (credits vary 1-3)
Prerequisite: Junior or senior standing and permission of the instructor and department chair.
Individual research on an approved subject may be taken for one to three credits.


[^0]:    * Support courses may change based on regulations from the Virginia Department of Education.

    Graduate courses* required (senior year):
    Select six credits from a), b), or c):
    a) MATH 570;
    b) PSYC/TCHG 544;
    c) MLAN 511, ENGL 530.

